



Lecture #22

Carnegie Mellon University

# ADVANCED DATABASE SYSTEMS

Vectorized Execution (Part II)

@Andy\_Pavlo // 15-721 // Spring 2018

# TODAY'S AGENDA

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Bit-Slicing

Bit-Weaving

Relaxed Operator Fusion (Prashanth)



# BITMAP ENCODING

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## *Original Data*

id	sex
1	M
2	M
3	M
4	F
6	M
7	F
8	M
9	M



# BITMAP ENCODING

## *Original Data*

id	sex
1	M
2	M
3	M
4	F
6	M
7	F
8	M
9	M



## *Compressed Data*

id	sex	
	M	F
1	1	0
2	1	0
3	1	0
4	0	1
6	1	0
7	0	1
8	1	0
9	1	0

# BITMAP INDEX: ENCODING

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## **Approach #1: Equality Encoding**

→ Basic scheme with one Bitmap per unique value.

## **Approach #2: Range Encoding**

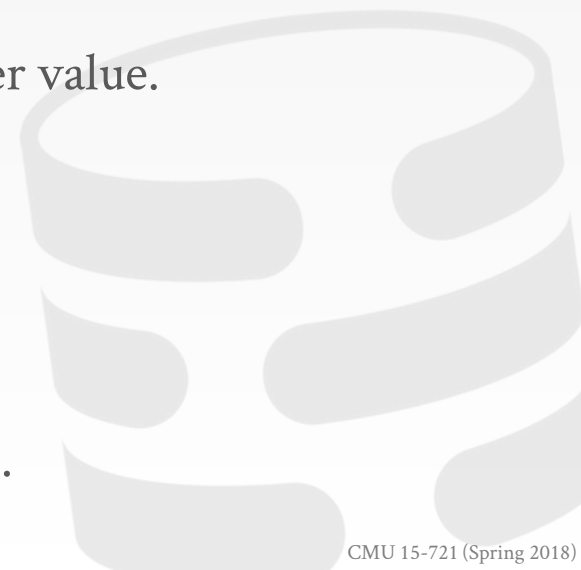
→ Use one Bitmap per interval instead of one per value.

## **Approach #3: Hierarchical Encoding**

→ Use a tree to identify empty key ranges.

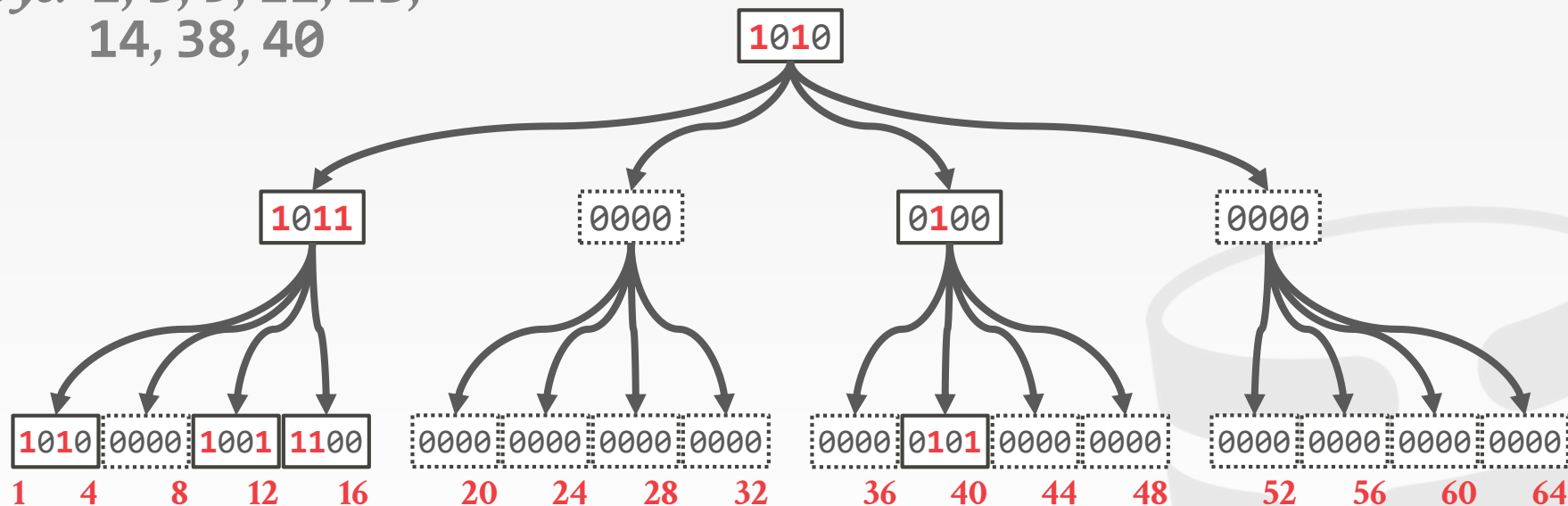
## **Approach #4: Bit-sliced Encoding**

→ Use a Bitmap per bit location across all values.



# HIERARCHICAL ENCODING

Keys: 1, 3, 9, 12, 13,  
14, 38, 40

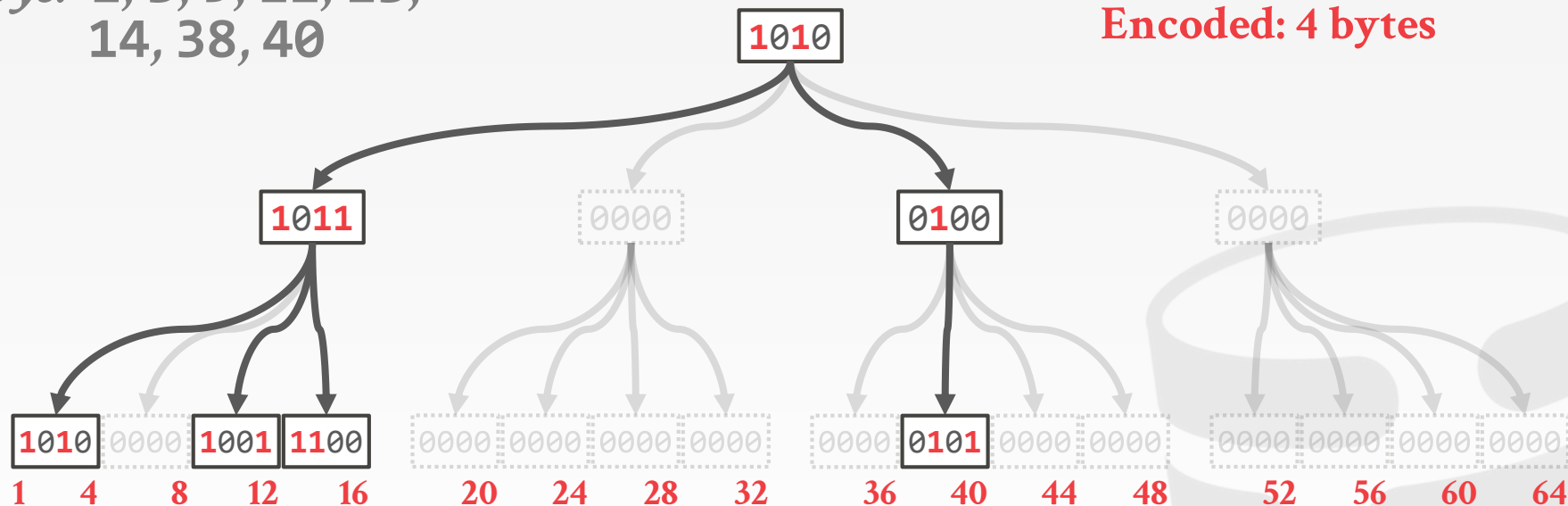


HIERARCHICAL BITMAP INDEX: AN EFFICIENT AND SCALABLE INDEXING TECHNIQUE FOR SET-VALUED ATTRIBUTES  
Advances in Databases and Information Systems 2003

# HIERARCHICAL ENCODING

Keys: 1, 3, 9, 12, 13,  
14, 38, 40

**Original: 8 bytes**  
**Encoded: 4 bytes**



HIERARCHICAL BITMAP INDEX: AN EFFICIENT AND SCALABLE INDEXING TECHNIQUE FOR SET-VALUED ATTRIBUTES  
Advances in Databases and Information Systems 2003

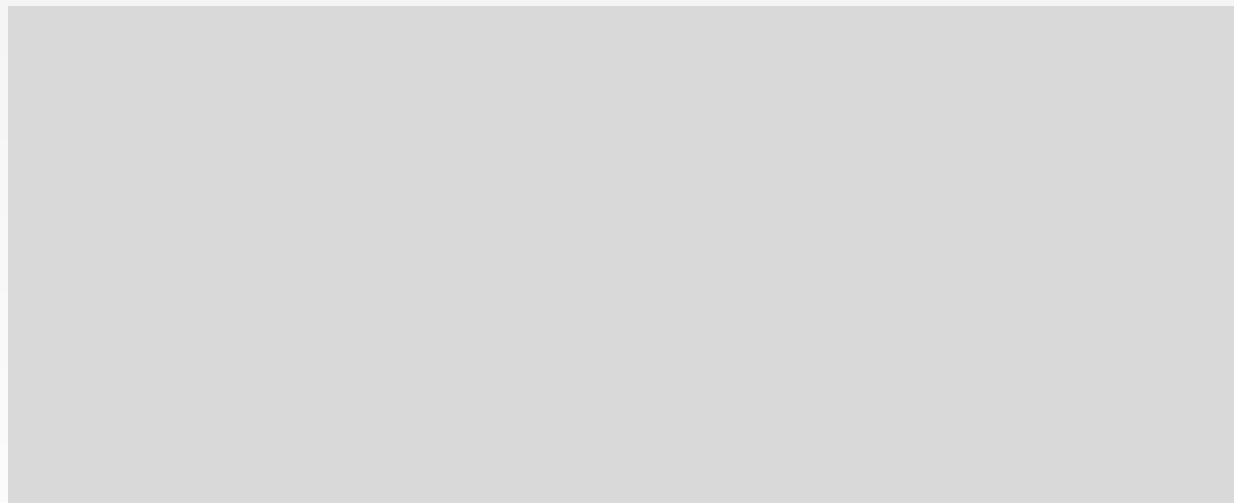
# BIT-SLICED ENCODING

---

## *Original Data*

id	zipcode
1	21042
2	15217
3	02903
4	90220
6	14623
7	53703

## *Bit-Slices*





# BIT-SLICED ENCODING

## Original Data

id	zipcode
1	21042
2	15217
3	02903
4	90220
6	14623
7	53703



## Bit-Slices

N? 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0

$\text{bin}(21042) \rightarrow 00101001000110010$

# BIT-SLICED ENCODING

## Original Data

id	zipcode
1	21042
2	15217
3	02903
4	90220
6	14623
7	53703



## Bit-Slices

N?	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0																	



$\text{bin}(21042) \rightarrow 00101001000110010$

# BIT-SLICED ENCODING

## Original Data

id	zipcode
1	21042
2	15217
3	02903
4	90220
6	14623
7	53703



## Bit-Slices

N?	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	0	1	0	0	1	0	0	0	1	1	0	0	1	0



$\text{bin}(21042) \rightarrow 00101001000110010$

# BIT-SLICED ENCODING

## Original Data

id	zipcode
1	21042
2	15217
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## Bit-Slices

N?	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	0	1	0	0	1	0	0	0	1	1	0	0	1	0
0	0	0	0	1	1	1	0	1	1	0	1	1	1	0	0	0	1
0	0	0	0	0	0	1	0	1	1	0	1	0	1	0	1	1	1
0	1	0	1	1	0	0	0	0	0	0	1	1	0	1	1	0	0
0	0	0	0	1	1	1	0	0	1	0	0	0	1	1	1	1	1
0	0	1	1	0	1	0	0	0	1	1	1	0	0	0	1	1	1

```
SELECT * FROM customer_dim
WHERE zipcode < 15217
```

# BIT-SLICED ENCODING

## Original Data

id	zipcode
1	21042
2	15217
3	02903
4	90220
6	14623
7	53703



## Bit-Slices

N?	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	0	1	0	0	1	0	0	0	1	1	0	0	1	0
0	0	0	0	1	1	1	0	1	1	0	1	1	1	0	0	0	1
0	0	0	0	0	0	1	0	1	1	0	1	0	1	0	1	1	1
0	1	0	1	1	0	0	0	0	0	0	1	1	0	1	1	0	0
0	0	0	0	1	1	1	0	0	1	0	0	0	1	1	1	1	1
0	0	1	1	0	1	0	0	0	1	1	1	0	0	0	1	1	1

```
SELECT * FROM customer_dim
WHERE zipcode < 15217
```

Walk each slice and construct a result bitmap.

# BIT-SLICED ENCODING

## Original Data

id	zipcode
1	21042
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## Bit-Slices

N?	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	0	1	0	0	1	0	0	0	1	1	0	0	1	0
0	0	0	0	1	1	1	0	1	1	0	1	1	1	0	0	0	1
0	0	0	0	0	0	1	0	1	1	0	1	0	1	0	1	1	1
0	1	0	1	1	0	0	0	0	0	0	1	1	0	1	1	0	0
0	0	0	0	1	1	1	0	0	1	0	0	0	1	1	1	1	1
0	0	1	1	0	1	0	0	0	1	1	1	0	0	0	1	1	1

```
SELECT * FROM customer_dim
WHERE zipcode < 15217
```

Walk each slice and construct a result bitmap.  
Skip entries that have 1 in first 3 slices (16, 15, 14)

# BIT-SLICED ENCODING

---

Bit-slices can also be used for efficient aggregate computations.

Example: **SUM(attr)**

- First, count the number of **1**s in **slice**<sub>17</sub> and multiply the count by  $2^{17}$
- Then, count the number of **1**s in **slice**<sub>16</sub> and multiply the count by  $2^{16}$
- Repeat for the rest of slices...

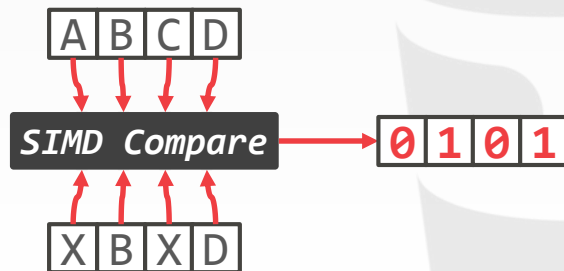
Intel added **POPCNT** SIMD instruction in 2008.

# OBSERVATION

The bit width of compressed data does not always fit naturally into SIMD register lanes.

→ This means that the DBMS has to do extra work to transform data into the proper format.

Just because the lanes are fully utilized does not mean the bits are fully utilized...



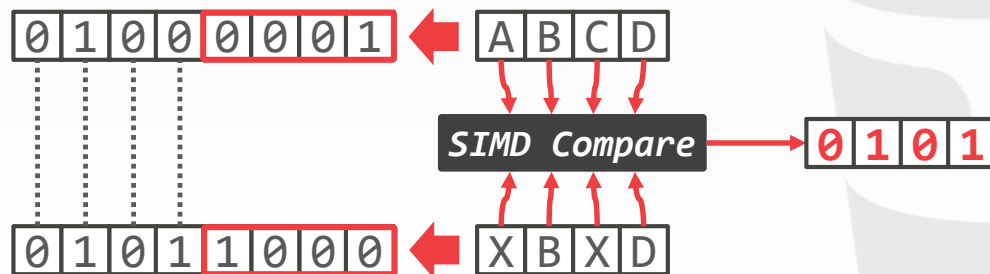


# OBSERVATION

The bit width of compressed data does not always fit naturally into SIMD register lanes.

→ This means that the DBMS has to do extra work to transform data into the proper format.

Just because the **lanes** are fully utilized does not mean the **bits** are fully utilized...



# BITWEAVING

---

Alternative storage layout for columnar databases that is designed for efficient predicate evaluation on compressed data using SIMD.

- Order-preserving dictionary encoding.
- Bit-level parallelization.
- Only require common instructions (no scatter/gather)

Implemented in Wisconsin's QuickStep engine.  
Became an Apache Incubator project in 2016.



BITWEAVING: FAST SCANS FOR MAIN  
MEMORY DATA PROCESSING  
SIGMOD 2013

# BITWEAVING

Alternative storage layout for columnar data that is designed for efficient processing on compressed data using SIMD.

- Order-preserving dictionary encoding.
- Bit-level parallelization.
- Only require common instructions.

Implemented in Wisconsin's Q  
Became an Apache Incubator project



BITWEAVING: FAST SCANS FOR MAIN  
MEMORY DATA PROCESSING  
SIGMOD 2013

# BITWEAVING – STORAGE LAYOUTS

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## **Approach #1: Horizontal**

→ Row-oriented storage at the bit-level

## **Approach #2: Vertical**

→ Column-oriented storage at the bit-level

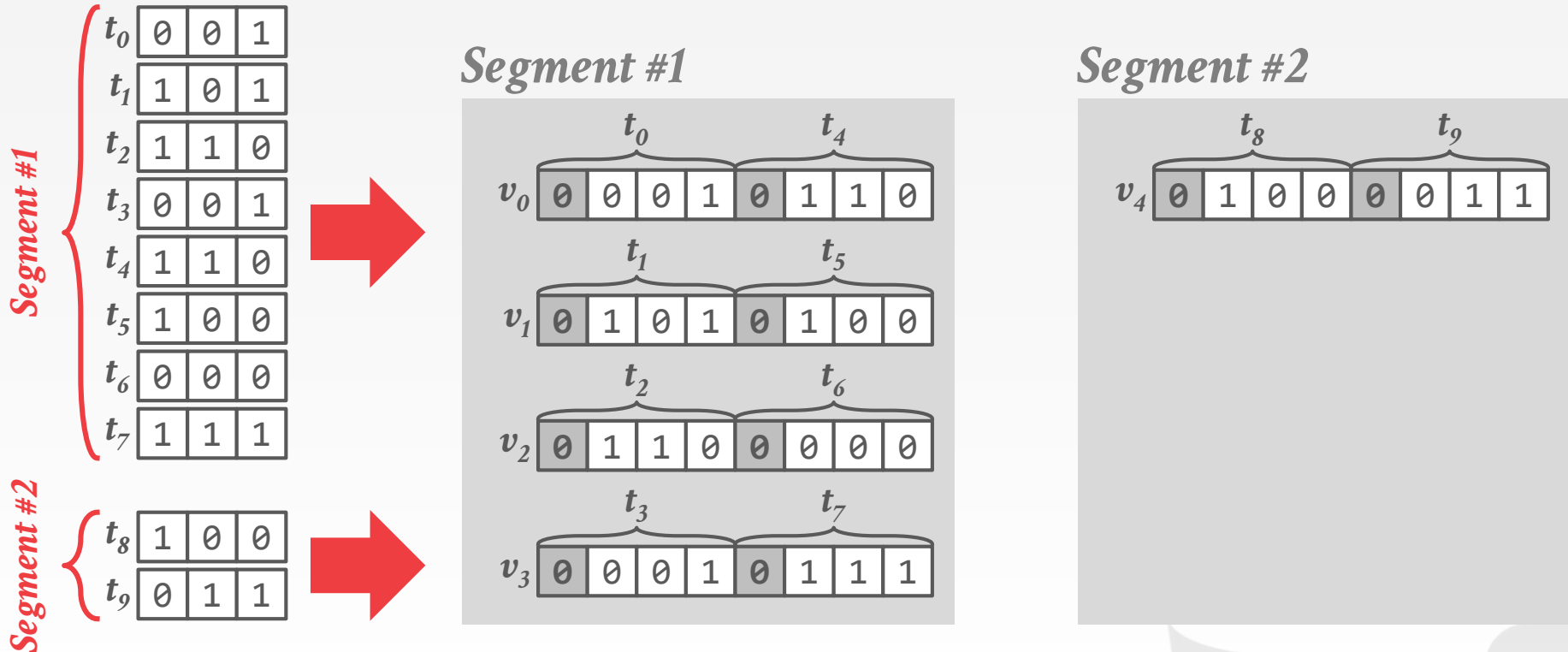


# HORIZONTAL STORAGE

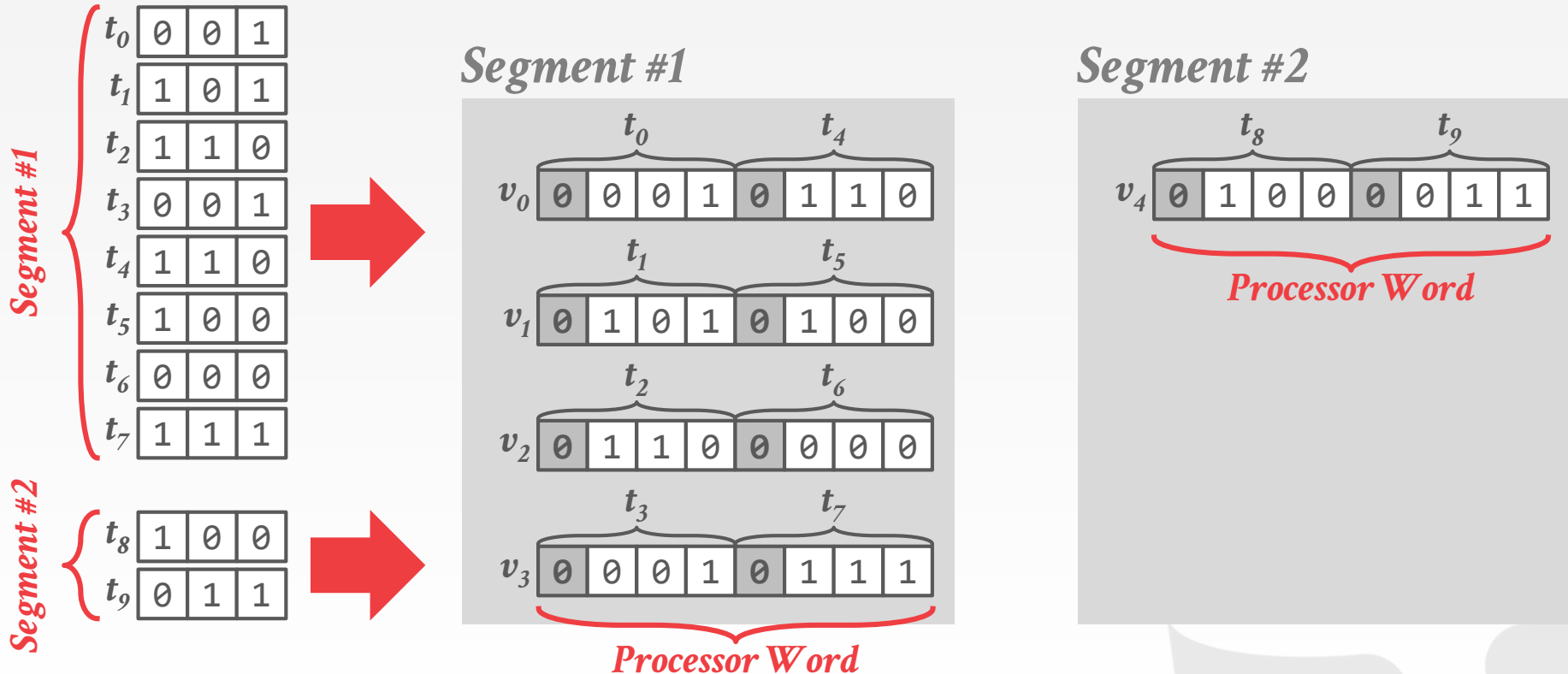
<i>Segment #1</i>	$t_0$	0	0	1	=1
	$t_1$	1	0	1	=5
	$t_2$	1	1	0	=6
	$t_3$	0	0	1	=1
	$t_4$	1	1	0	=6
	$t_5$	1	0	0	=4
	$t_6$	0	0	0	=0
	$t_7$	1	1	1	=7
<i>Segment #2</i>	$t_8$	1	0	0	=4
	$t_9$	0	1	1	=3



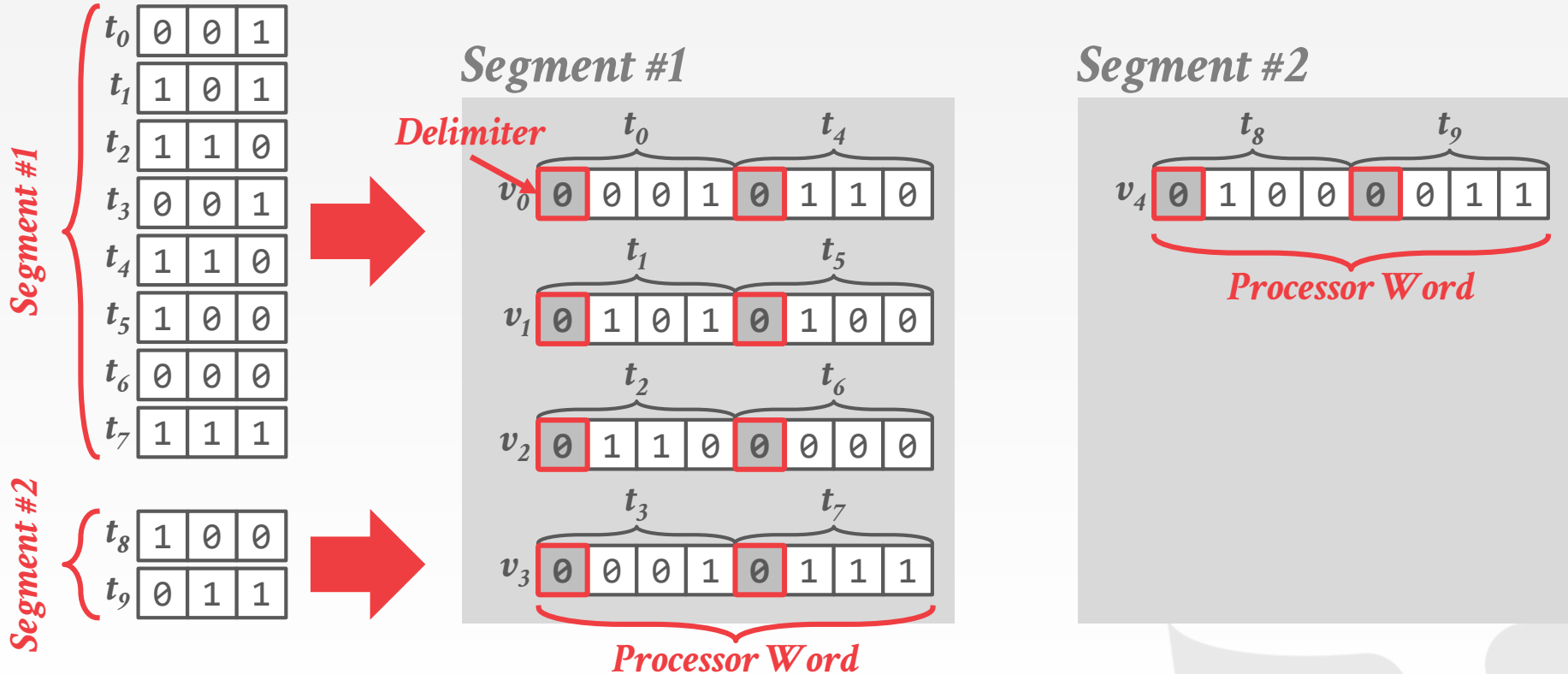
# HORIZONTAL STORAGE



# HORIZONTAL STORAGE



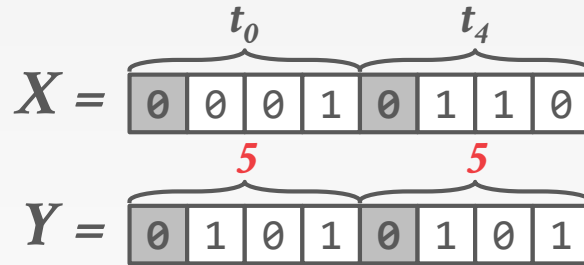
# HORIZONTAL STORAGE





# BITWEAVING/H – EXAMPLE

```
SELECT * FROM table
WHERE val < 5
```



# BITWEAVING/H – EXAMPLE

```
SELECT * FROM table
WHERE val < 5
```

$$X = \begin{array}{|c|c|c|c|c|c|c|c|} \hline & \underbrace{\phantom{0001}}_{t_0} & & \underbrace{\phantom{0110}}_{t_4} & & & & \\ \hline 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ \hline \end{array}$$

$$Y = \begin{array}{|c|c|c|c|c|c|c|c|} \hline & \underbrace{\phantom{0101}}_5 & & \underbrace{\phantom{0101}}_5 & & & & \\ \hline 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ \hline \end{array}$$

$$\text{mask} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ \hline \end{array}$$

$$(Y + (X \oplus \text{mask})) \wedge \neg \text{mask} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline \end{array}$$



# BITWEAVING/H – EXAMPLE

```
SELECT * FROM table
WHERE val < 5
```

$$X = \begin{array}{|c|c|c|c|c|c|c|c|} \hline & \underbrace{\phantom{0\ 0\ 0\ 1}}_{t_0} & & \underbrace{\phantom{0\ 1\ 1\ 0}}_{t_4} & & & & \\ \hline 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ \hline \end{array}$$

$$Y = \begin{array}{|c|c|c|c|c|c|c|c|} \hline & \underbrace{\phantom{0\ 1\ 0\ 1}}_5 & & \underbrace{\phantom{0\ 1\ 0\ 1}}_5 & & & & \\ \hline 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ \hline \end{array}$$

$$\text{mask} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ \hline \end{array}$$

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*Selection Vector*



# BITWEAVING/H – EXAMPLE

```
SELECT * FROM table
WHERE val < 5
```

$$X = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{0} & \text{0} & \text{0} & \text{1} & \text{0} & \text{1} & \text{1} & \text{0} \\ \hline \end{array}$$

$t_0$                        $t_4$

$$Y = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{0} & \text{1} & \text{0} & \text{1} & \text{0} & \text{1} & \text{0} & \text{1} \\ \hline \end{array}$$

$5$                        $5$

$$\text{mask} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{0} & \text{1} & \text{1} & \text{1} & \text{0} & \text{1} & \text{1} & \text{1} \\ \hline \end{array}$$

$$(Y + (X \oplus \text{mask})) \wedge \neg \text{mask} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{1} & \text{0} & \text{0} & \text{0} & \text{0} & \text{0} & \text{0} & \text{0} \\ \hline \end{array}$$

$1 < 5$                        $5 < 6$



# BITWEAVING/H – EXAMPLE

```
SELECT * FROM table
WHERE val < 5
```

$$X = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{0} & \text{0} & \text{0} & \text{1} & \text{0} & \text{1} & \text{1} & \text{0} \\ \hline \end{array}$$

$t_0$                        $t_4$

$5$                        $5$

$$Y = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{0} & \text{1} & \text{0} & \text{1} & \text{0} & \text{1} & \text{0} & \text{1} \\ \hline \end{array}$$

$$\text{mask} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{0} & \text{1} & \text{1} & \text{1} & \text{0} & \text{1} & \text{1} & \text{1} \\ \hline \end{array}$$

$$(Y + (X \oplus \text{mask})) \wedge \neg \text{mask} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{1} & \text{0} & \text{0} & \text{0} & \text{0} & \text{0} & \text{0} & \text{0} \\ \hline \end{array}$$

$1 < 5$                        $5 < 6$

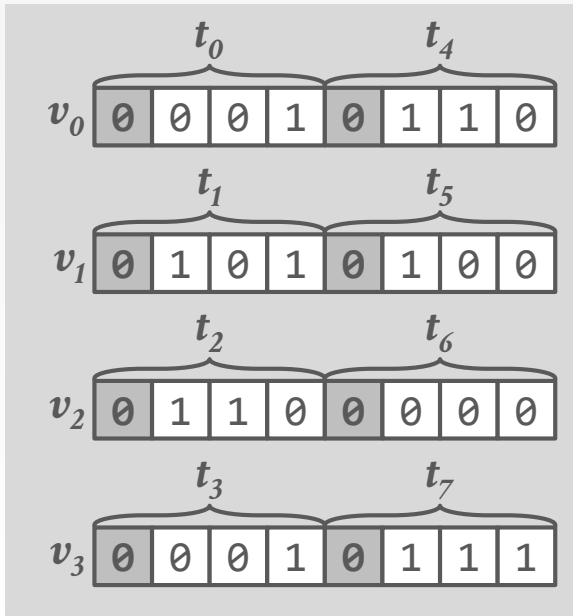
Only requires three instructions to evaluate a single word.

Works on any word size and encoding length.

Paper contains algorithms for other operators.

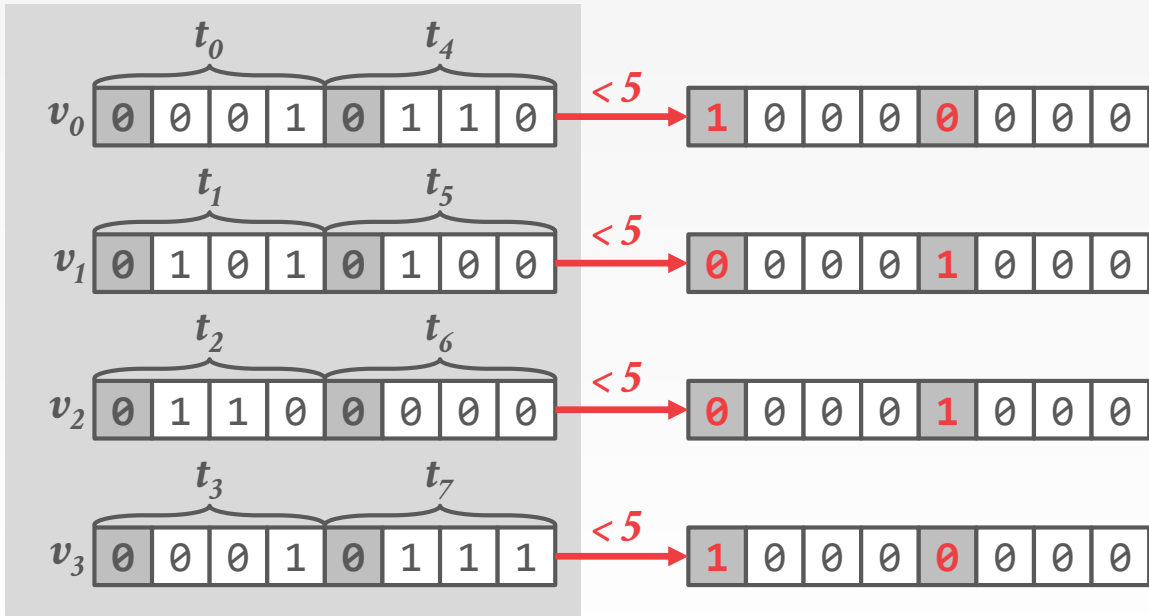
# BITWEAVING/H – EXAMPLE

```
SELECT * FROM table
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```



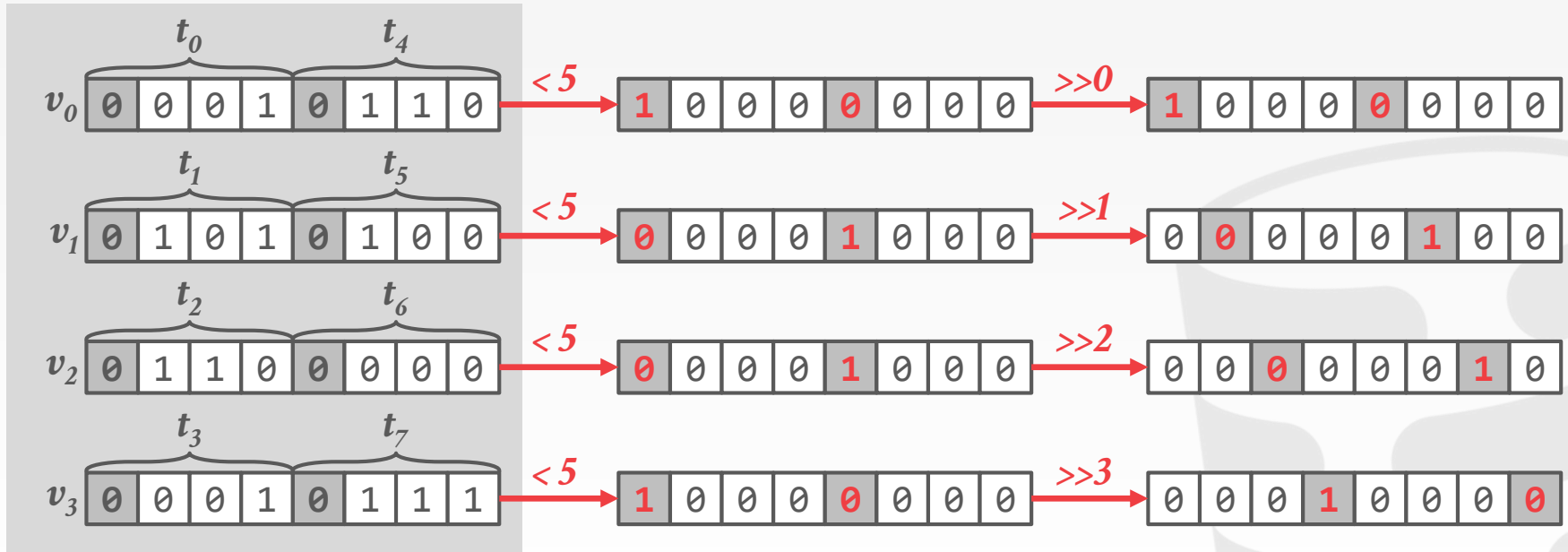
# BITWEAVING/H – EXAMPLE

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SELECT * FROM table
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# BITWEAVING/H – EXAMPLE

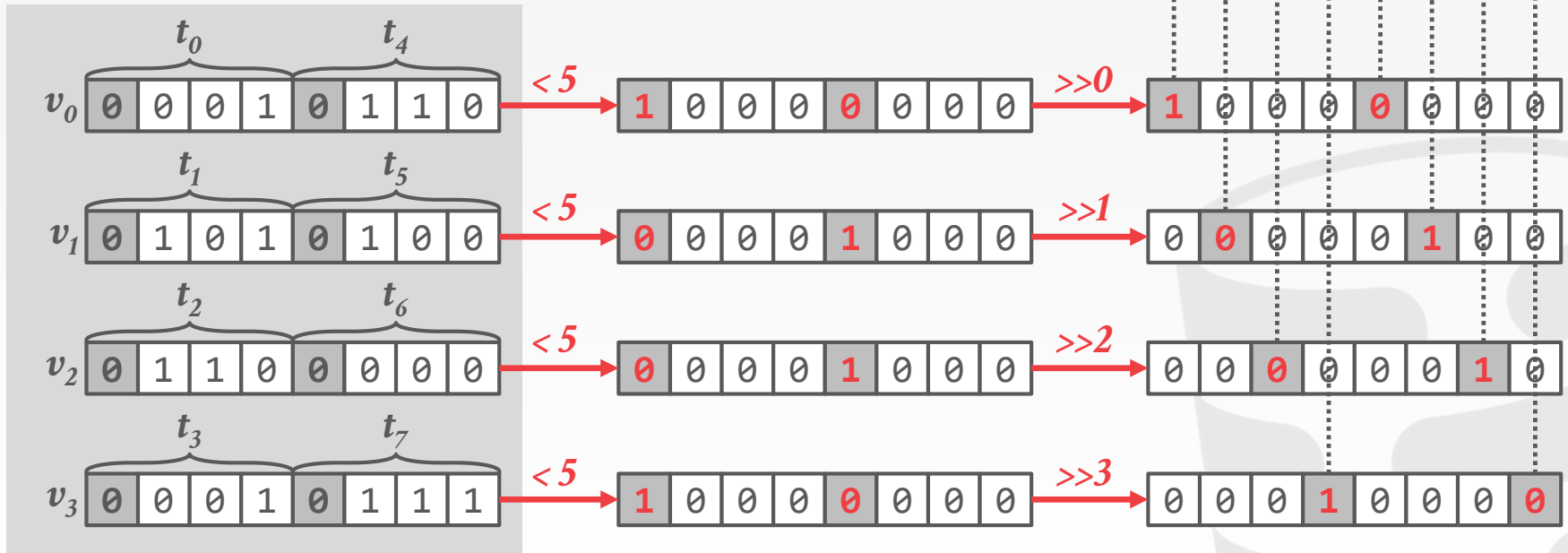
```
SELECT * FROM table
WHERE val < 5
```





# BITWEAVING/H – EXAMPLE

```
SELECT * FROM table
WHERE val < 5
```



# SELECTION VECTOR

---

SIMD comparison operators produce a bit mask that specifies which tuples satisfy a predicate.

Have to convert it into offsets / positions.

- Approach #1: Iteration
- Approach #2: Pre-compute Positions Table



# SELECTION VECTOR

---

SIMD comparison operators produce a bit mask that specifies which tuples satisfy a predicate.

Have to convert it into offsets / positions.

→ Approach #1: Iteration

→ Approach #2: Pre-compute Positions Table

	$t_0$	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$
<i>Selection Vector</i>	1	0	0	1	0	1	1	0



# SELECTION VECTOR

---

SIMD comparison operators produce a bit mask that specifies which tuples satisfy a predicate.

Have to convert it into offsets / positions.

→ Approach #1: Iteration

→ Approach #2: Pre-compute Positions Table

*Selection Vector*

$t_0$	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$
1	0	0	1	0	1	1	0

```
tuples = [ ]
for (i=0; i<n; i++) {
  if sv[i] == 1
    tuples.add(i);
}
```

# SELECTION VECTOR

---

SIMD comparison operators produce a bit mask that specifies which tuples satisfy a predicate.

Have to convert it into offsets / positions.

→ Approach #1: Iteration

→ Approach #2: Pre-compute Positions Table

	$t_0$	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$
<i>Selection Vector</i>	1	0	0	1	0	1	1	0



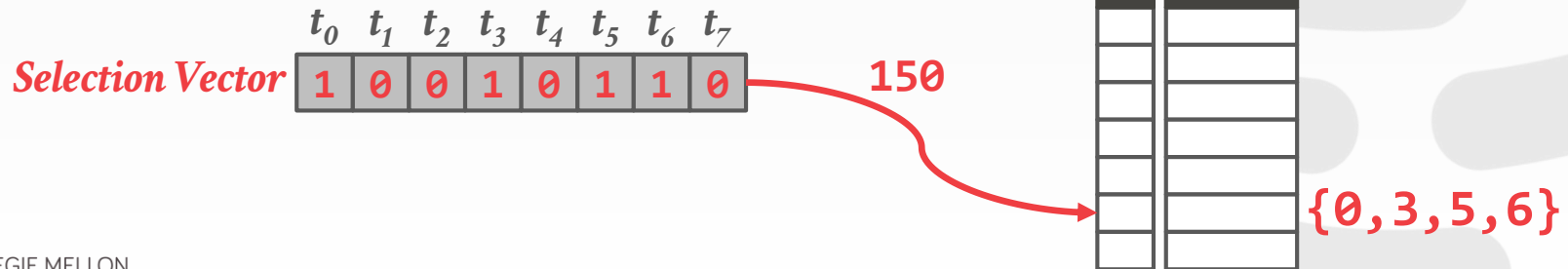
# SELECTION VECTOR

SIMD comparison operators produce a bit mask that specifies which tuples satisfy a predicate.

Have to convert it into offsets / positions.

→ Approach #1: Iteration

→ Approach #2: Pre-compute Positions Table



# VERTICAL STORAGE

<i>Segment #1</i>	$t_0$	0	0	1
	$t_1$	1	0	1
	$t_2$	1	1	0
	$t_3$	0	0	1
	$t_4$	1	1	0
	$t_5$	1	0	0
	$t_6$	0	0	0
	$t_7$	1	1	1
<i>Segment #2</i>	$t_8$	1	0	0
	$t_9$	0	1	1



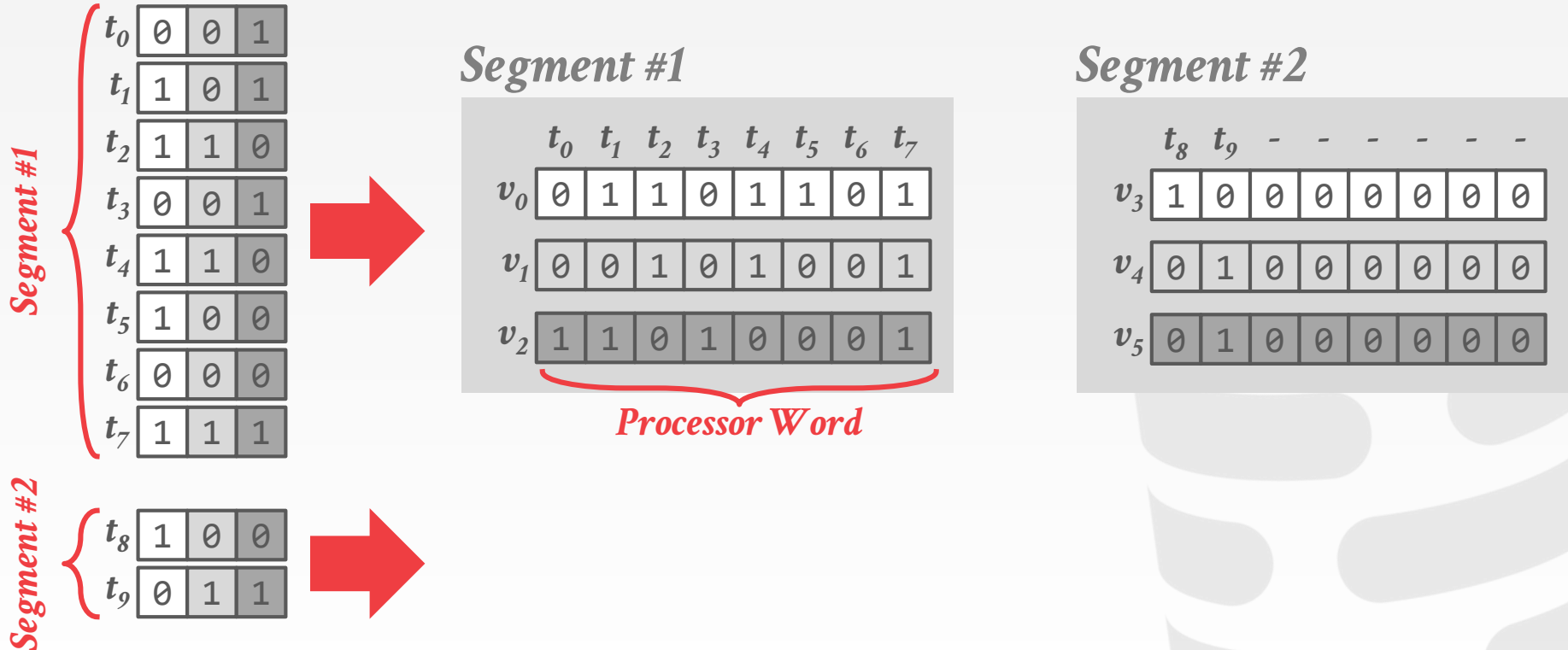
# VERTICAL STORAGE

<i>Segment #1</i>	$t_0$	0	0	1
	$t_1$	1	0	1
	$t_2$	1	1	0
	$t_3$	0	0	1
	$t_4$	1	1	0
	$t_5$	1	0	0
	$t_6$	0	0	0
	$t_7$	1	1	1
<i>Segment #2</i>	$t_8$	1	0	0
	$t_9$	0	1	1





# VERTICAL STORAGE



# BITWEAVING/V – EXAMPLE

```
SELECT * FROM table  
WHERE key = 2
```

## Segment #1

	$t_0$	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$
$v_0$	0	1	1	0	1	1	0	1
$v_1$	0	0	1	0	1	0	0	1
$v_2$	1	1	0	1	0	0	0	1



# BITWEAVING/V – EXAMPLE

```
SELECT * FROM table
WHERE key = 2
```

0 1 0

*Segment #1*

	$t_0$	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$
$v_0$	0	1	1	0	1	1	0	1
$v_1$	0	0	1	0	1	0	0	1
$v_2$	1	1	0	1	0	0	0	1



# BITWEAVING/V – EXAMPLE

```
SELECT * FROM table
WHERE key = 2
```

0 1 0

0 0 0 0 0 0 0 0

**SIMD Compare**

1 0 0 1 0 0 1 0

*Segment #1*

$t_0$   $t_1$   $t_2$   $t_3$   $t_4$   $t_5$   $t_6$   $t_7$

$v_0$  0 1 1 0 1 1 0 1

$v_1$  0 0 1 0 1 0 0 1

$v_2$  1 1 0 1 0 0 0 1



# BITWEAVING/V – EXAMPLE

```
SELECT * FROM table
WHERE key = 2
```

0 1 0

*Segment #1*

	$t_0$	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	$t_7$
$v_0$	0	1	1	0	1	1	0	1
$v_1$	0	0	1	0	1	0	0	1
$v_2$	1	1	0	1	0	0	0	1

1 1 1 1 1 1 1 1

*SIMD Compare*

1 0 0 1 0 0 1 0

*SIMD Compare*

0 0 0 0 0 0 0 0

Can perform early pruning just like in BitMap indexes.

The last vector is skipped because all bits in previous comparison are zero.

# EVALUATION

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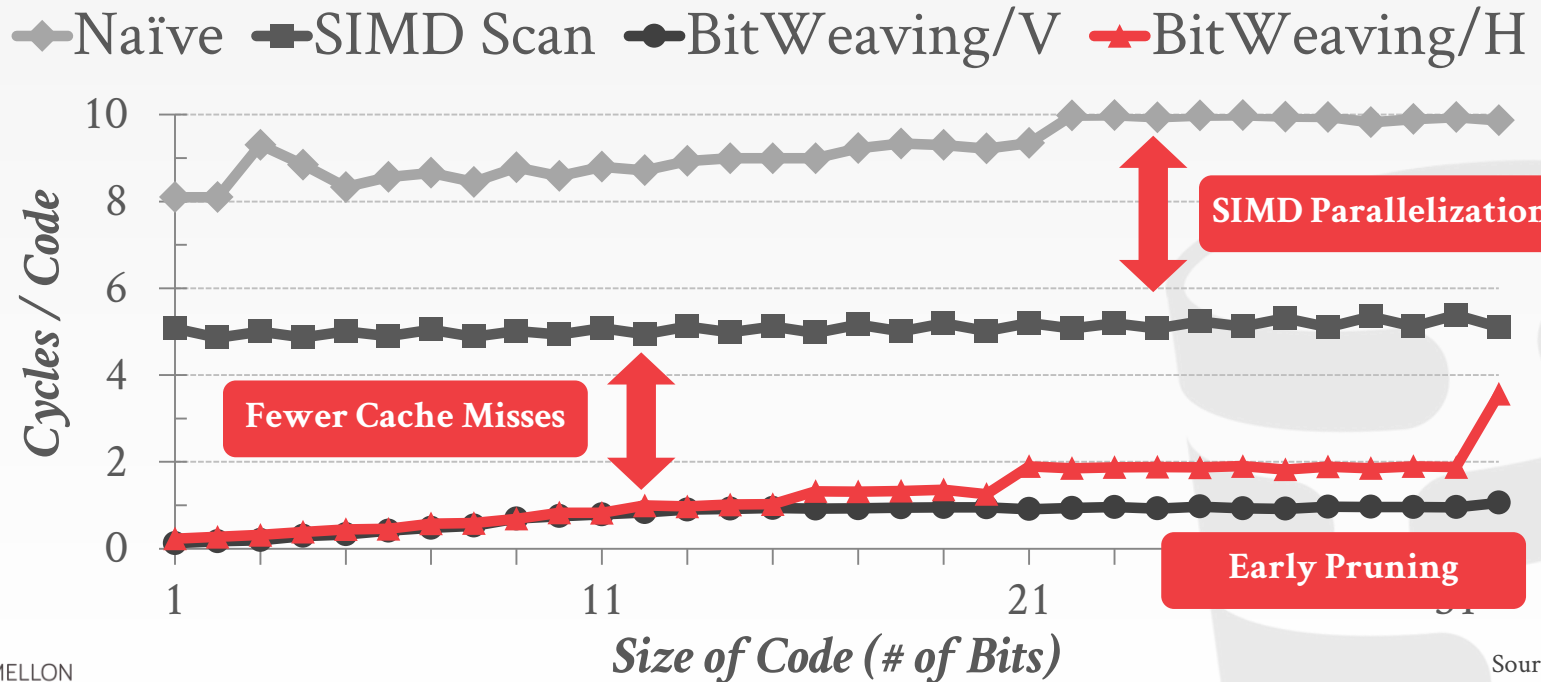
Single-threaded execution of a single query derived from TPC-H benchmark.  
→ Selectivity: 10%

10GB TPC-H Database  
→ 1 billion tuples  
→ Uniform distribution

```
SELECT COUNT(*)  
FROM R  
WHERE R.a < C
```

# EVALUATION

*TPC-H Aggregation Query*  
*Intel Xeon X5650 @ 2.66 GHz*



# PARTING THOUGHTS

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Just like in query compilation, getting the best performance with vectorization requires the DBMS to store data in a way that is best for the CPU and not the best for humans' understanding.

